CSE 6242/CX 4242

Graphs / Networks

Centrality measures, algorithms, interactive applications

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> Partly based on materials by Professors Guy Lebanon, Jeffrey Heer, John Stasko, Christos Faloutsos, Le Song

Recap...

- Last time: Basics, how to build graph, store graph, laws, etc.
- Today: Centrality measures, algorithms, interactive applications for visualization and recommendation

Centrality = "Importance"

Why Node Centrality?

What can we do if we can rank all the nodes in a graph (e.g., Facebook, LinkedIn, Twitter)?

- Find celebrities or influential people in a social network (Twitter)
- Find "gatekeepers" who connect communities (headhunters love to find them on LinkedIn)
- What else?



More generally

Helps graph analysis, visualization, understanding, e.g.,

- Let us rank nodes, group or study them by centrality
- Only show subgraph formed by the top 100 nodes, out of the millions in the full graph
 - Similar to google search results (ranked, and they only show you 10 per page)
- Most graph analysis packages already have centrality algorithms implemented. Use them!

Can also compute edge centrality. Here we focus on node centrality.

Degree Centrality (easiest)

Degree = number of neighbors

- For directed graphs
 - In degree = No. of incoming edges
 - Out degree = No. of outgoing edges
- For undirected graphs, only degree is defined.
- Algorithms?
 - Sequential scan through edge list
 - What about for a graph stored in SQLite?

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Computing Degrees using SQL

Recall simplest way to store a graph in SQLite:

edges(source_id, target_id)

- 1. If slow, first create index for each column
- 2. Use group by statement to find in degrees

select count(*) from edges group by source_id;

Betweenness Centrality

High betweenness = "gatekeeper"

Betweenness of a node v

 $= \sum_{\substack{s \neq v \neq t \in V}} \frac{\sigma_{st}(v)}{\sigma_{st}}$

Number of shortest paths between s and t that goes through v

Number of shortest paths between s and t

= how often a node serves as the "bridge" that connects two other nodes.

(Local) Clustering Coefficient

A node's clustering coefficient is a measure of how close the node's neighbors are from forming a clique.

- 1 = neighbors form a clique
- 0 = No edges among neighbors

(Assuming undirected graph)

"Local" means it's for a node; can also compute a graph's "global" coefficient



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Computing Clustering Coefficients...

Requires triangle counting

Real social networks have a lot of triangles

• Friends of friends are friends

Triangles are **expensive** to compute

(neighborhood intersections; several approx. algos)

Can we do that quickly?

Algorithm details: Faster Clustering Coefficient Using Vertex Covers <u>http://www.cc.gatech.edu/~ogreen3/_docs/2013VertexCoverClusteringCoefficients.pdf</u>

Super Fast Triangle Counting [Tsourakakis ICDM 2008]



But: triangles are expensive to compute (3-way join; several approx. algos) Q: Can we do that quickly? A: Yes! #triangles = 1/6 Sum (λ_i³)

(and, because of skewness, we only need the top few eigenvalues!

Power Law in Eigenvalues of Adjacency Matrix





1000x+ speed-up, >90% accuracy

More Centrality Measures...

- Degree
- Betweenness
- Closeness, by computing
 - Shortest paths
 - "Proximity" (usually via random walks) used successfully in a lot of applications
- Eigenvector



PageRank (Google)



Larry Page

Sergey Brin

Brin, Sergey and Lawrence Page (1998). Anatomy of a Large-Scale Hypertextual Web Search Engine. 7th Intl World Wide Web Conf.

PageRank: Problem

Given a directed graph, find its most interesting/central node



A node is important, if it is connected with important nodes (recursive, but OK!)

PageRank: Solution

Given a directed graph, find its most interesting/central node

Proposed solution: use **random walk**; spot most 'popular' node (-> steady state probability (ssp))



"state" = webpage

A node has high ssp, if it is connected with high ssp nodes (recursive, but OK!)

Let **B** be the transition matrix: transposed, column-normalized







		1			p1
1			1		p2
	1/2			1/2	p3
				1/2	p4
	1/2				p5
<u> </u>					

B



p

p

- **B** p = 1 * p
- thus, p is the eigenvector that corresponds to the highest eigenvalue (=1, since the matrix is column-normalized)
- Why does such a p exist?
 - p exists if B is nxn, nonnegative, irreducible
 [Perron–Frobenius theorem]

- In short: imagine a particle randomly moving along the edges
- compute its steady-state probability (ssp)

Full version of algorithm: with occasional random jumps Why? To make the matrix irreducible

Full Algorithm

- With probability *1-c*, fly-out to a random node



http://williamcotton.com/pagerank-explained-with-javascript

PageRank Explained with Javascript



How to compute PageRank for huge matrix?

Use the power iteration method

http://en.wikipedia.org/wiki/Power_iteration

p

p = c B p + (1-c)/n 1

B

p



Can initialize this vector to any non-zero vector, e.g., all "1"s

PageRank for graphs (generally)

You can compute PageRank for any graphs

Should be in your algorithm "toolbox"

- Better than simple centrality measure (e.g., degree)
- Fast to compute for large graphs (O(E))

But can be "misled" (Google Bomb)

• How?

Personalized PageRank

Make one small variation of PageRank

- Intuition: not all pages are equal, some more relevant to a person's specific needs
- How?

"Personalizing" PageRank

 With probability 1-c, fly-out to a random node some preferred nodes



Why learn Personalized PageRank?

Can be used for **recommendation**, e.g.,

- If I like this webpage, what would I also be interested?
- If I like this product, what other products I also like? (in a user-product bipartite graph)
- Also helps with visualizing large graphs
 - Instead of visualizing every single nodes, visualize the most important ones

Again, very flexible. Can be run on any graph.

Building an interactive application

Will show you an example application (Apolo) that uses a "diffusion-based" algorithm to perform recommendation on a large graph

Personalized PageRank

(= Random Walk with Restart)

- Belief Propagation (powerful inference algorithm, for fraud detection, image segmentation, error-correcting codes, etc.)
- "Spreading activation" or "degree of interest" in Human-Computer Interaction (HCI)
- Guilt-by-association techniques

Building an interactive application

Why diffusion-based algorithms are widely used?

- Intuitive to interpret uses "network effect", homophily, etc.
- Easy to implement Math is relatively simple
- Fast

run time linear to #edges, or better

Probabilistic meaning

Human-In-The-Loop Graph Mining **Apolo:** Machine Learning + Visualization *CHI 2011*

Apolo: Making Sense of Large Network Data by Combining Rich User Interaction and Machine Learning

Finding More Relevant Nodes



Finding More Relevant Nodes



Citation network

Finding More Relevant Nodes



Citation network

Apolo uses guilt-by-association (Belief Propagation, similar to personalized PageRank)

Demo: Mapping the Sensemaking Literature

Nodes: 80k papers from Google Scholar (node size: #citation) Edges: 150k citations



The cost structure of sensemaking

Russell, D.M. and Stefik, M.J. and Pirolli, P. and Card, S.K.

245 citations 8 versions

PDF 1993

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Key Ideas (Recap)

Specify exemplars Find other relevant nodes (BP)



Apolo's Contributions 1 Human + Machine

It was like having a **partnership** with the machine.

2 Personalized Landscape

Apolo 2009

Cluster Data Add Group

Recommendations

End User Programming

End users creating effective softw... End user software engineering: chi... Invited research overview: end-us... Brad A. Myers

Margaret M. Burnett Mary Beth Rosson Andrew Jensen Ko Alan F. Blackwell

Text Entry

In-stroke word completion. Integrating isometric joysticks into... Eyes on the road, hands on the whe... An alternative to push, press, and t... Maximizing the guessability of symb... Few-key text entry revisited: mnem... Text entry from power wheelchairs: ... Joystick text entry with date stamp, ... Hudding on the stamp, ...

Not Interested

Automatically generating user inte...

•

Decision-Theoretic User Daniel S. Weld

Krzysztof Z. Gajos Automatically generating Exploring the design space Predictability and accuracy

Brad

Brad A. Myers

The garnet user interface developm... Using HCI Techniques to Design a M... Creating charts by demonstration. The Amulet User Interface Developm... Easily Adding Animations to Interfac... Simplifying video editng using metad... SILVER: simplifying video editing wit...

Interface Generation

Huddle: automatically generating i... UNIFORM: automatically generatin... Demonstrating the viability of auto... Jeffrey Nichols Brandon Rothrock Duen Horng Chau -

Apolo 2010

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CiteSense: supporting sensemaking 0 Zhang, X. 2008 An informal information-seeking e 53 Hendry, [1997 17 nodes selected	Change in Representations
An empirical evaluation of user into 35 Amento, 1999 The effectiveness of automatically 19 Gon{\c[c 2004] The microstructures of social taggi 3 Fu, W.T. 2008 Sensemaking: Bringing theories an 0 Sharma, I 2006 Data manipulation services in the F 7 Asdoorial 1998 Considerations for information env. 78 Furnas, G 1998 Improve results Considerations for information env. 78 Furnas, G 1998 Improve results Constitute Proceedings of the INTER-	aking , Card, S.K.

Apolo 2011 22,000 lines of code. Java 1.6. Swing. Uses SQLite3 to store graph on disk



245 citations 8 versions

User Study

Used citation network

Task: Find related papers for 2 sections in a survey paper on *user interface*

- Model-based generation of UI
- Rapid prototyping tools

Past, Present and Future of User Interface Software Tools

Brad Myers, Scott E. Hudson, and Randy Pausch

Human Computer Interaction Institute School of Computer Science Carnegie Mellon University

Apolo Google Scholar

Between subjects design Participants: grad student or research staff

Google Scholar Apolo P **N** ſ٩) ſ٩) ſ٩) [⁴] "Model-based" "Prototyping" [予 [予 [予 ſ٩) ſ٩) ſ٩Ì ſ٩ ٢Ĵ ſ٩) ſ٩) 10 papers for each section

> Expert judges rated papers





* Statistically significant, by two-tailed t test, p <0.05

Apolo: Recap

A mixed-initiative approach for exploring and creating personalized landscape for large network data

Apolo = ML + Visualization + Interaction



Practitioners' guide to building (interactive) applications

Think about scalability early

• e.g., picking a scalable algorithm early on

When building interactive applications, use **iterative** design approach (as in Apolo)

- Why? It's hard to get it right the first time
- Create prototype, evaluate, modify prototype, evaluate, ...
- Quick evaluation helps you identify important fixes early (can save you a lot of time)

Practitioners' guide to building (interactive) applications

How to do **iterative** design?

What kinds of **prototypes**?

• Paper prototype, lo-fi prototype, high-fi prototype

What kinds of evaluation? Important to involve REAL users as early as possible

- Recruit your friends to try your tools
- Lab study (controlled, as in Apolo)
- Longitudinal study (usage over months)
- Deploy it and see the world's reaction!
- To learn more:
 - CS 6750 Human-Computer Interaction
 - CS 6455 User Interface Design and Evaluation

Polonium: Web-Scale Malware Detection *SDM 2011*

Polonium: Tera-Scale Graph Mining and Inference for Malware Detection

Typical Malware Detection Method

Signature-based detection
1.Collect malware
2.Generate signatures
3.Distribute to users
4.Scan computers for matches



What about "zero-day" malware? No samples \rightarrow No signatures \rightarrow No detection How to detect them early?



Reputation-Based Detection

Computes reputation score for each application e.g., MSWord.exe

Poor reputation = Malware



Patented

I led initial design and development Serving 120 million users Answered trillions of queries

Propagation of leverage of <u>network influence</u> unearths malware

Patented

I led initial design and development Serving 120 million users Answered trillions of queries

Polonium works with 60 Terabyte Data

50 million machines

900 million unique files

(Identified by their cryptographic hash values)

Goal: label malware and good files

Why A Hard Problem?

Existing Research	Polonium
Small dataset	Huge dataset (60 terabytes)
Detects specific malware (e.g., worm, trojans)	Detects all types (needs a general method)
Many false alarms (>10%)	Strict (<1%)

Polonium: Problem Definition

Given

Undirected machine-file bipartite graph

37 billion edges, **1 billion** nodes (machines, files) Some file labels from Symantec (**good** or **bad**)

Find

Labels for all **unknown** files

Where to Get Good and Bad Labels?

Symantec has a **ground truth database** of **known-good** and **known-bad** files

e.g., set known-good file's prior to 0.9

How to Gauge Machine Reputation?

Computed using Symantec's proprietary formula; a value between 0 and 1

Derived from anonymous aspects of machine's usage and behavior

How to propagate known information to the unknown?

Key Idea: Guilt-by-Association

GOOD files likely appear on GOOD machines BAD files likely appear on BAD machines Also known as Homophily

Machine

How to propagate known information to the unknown?

Adapts **Belief Propagation (BP)**

A powerful inference algorithm

Used in image processing, computer vision, error-correcting codes, etc.

Two Equations in Belief Propagation

Details

$$b_i(x_i) = k\phi(x_i) \prod_{x_j \in N(i)} m_{ji}(x_i)$$

$$m_{ij}(x_j) \leftarrow \sum_{x_i \in X} \psi_{ij}(x_i, x_j) \phi(x_i) \prod_{k \in N(i) \setminus j} m_{ki}(x_i)$$

Computing Node Belief (Reputation)

Details

$b_i(x_i) = k\phi(x_i) \prod_{x_j \in N(i)} m_{ji}(x_i)$

Computing Node Belief (Reputation)

Details

$$b_{i}(x_{i}) = k\phi(x_{i}) \prod_{x_{j} \in N(i)} m_{ji}(x_{i})$$

Belief Prior belief Neighbors' opinions

Computing Node Belief (Reputation)

$$b_{i}(x_{i}) = k\phi(x_{i}) \prod_{x_{j} \in N(i)} m_{ji}(x_{i})$$

Belief Prior belief Neighbors' opinions
Creating Message for Neighbor



$m_{ij}(x_j) \leftarrow \sum_{x_i \in X} \psi_{ij}(x_i, x_j) \phi(x_i) \prod_{k \in N(i) \setminus j} m_{ki}(x_i)$

Creating Message for Neighbor



$$m_{ij}(x_j) \leftarrow \sum_{x_i \in X} \psi_{ij}(x_i, x_j) \phi(x_i) \prod_{k \in N(i) \setminus j} m_{ki}(x_i)$$
Opinion for neighbor Edge potential Belief
$$\frac{6000 \text{ Bad}}{6000 \text{ 0.9 0.1}}$$
Bad 0.1 0.9

Creating Message for Neighbor



Evaluation

Using millions of ground truth files, 10-fold cross validation



Evaluation

Using millions of ground truth files, 10-fold cross validation









Scalability How Did I Scale Up BP?

- 1.Early termination (after 6 iterations) \rightarrow Faster
- 2.Keep edges on disk \rightarrow Saves 200GB of RAM
- 3.Computes half of the messages \rightarrow Twice as fast

Further Scale Up Belief Propagation Use **Hadoop** if graph doesn't fit in memory [ICDE'11] Speed scales up **linearly** with number of machines

